

# Multi-task deep learning with optical flow features for self-driving cars

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**Abstract:** The control of self-driving cars has received growing attention recently. Although existing research shows promising results in the vehicle control using video from a monocular dash camera, there has been very limited work on directly learning vehicle control from motion-based cues. Such cues are powerful features for visual representations, as they encode the per-pixel movement between two consecutive images, allowing a system to effectively map the features into the control signal. The authors propose a new framework that exploits the use of a motion-based feature known as *optical flow* extracted from the dash camera and demonstrates that such a feature is effective in significantly improving the accuracy of the control signals. The proposed framework involves two main components. The flow predictor, as a self-supervised deep network, models the underlying scene structure from consecutive frames and generates the optical flow. The controller, as a supervised multi-task deep network, predicts both steer angle and speed. The authors demonstrate that the proposed framework using the optical flow features can effectively predict control signals from a dash camera video. Using the Cityscapes data set, the authors validate that the system prediction has errors as low as 0.0130 rad/s on steer angle and 0.0615 m/s on speed, outperforming existing research.

## 1 Introduction

Self-driving vehicles have attracted much attention due to the prospect of driving robustly without human involvement in the controls. To achieve this, the ability to analyse the environment using data coming from sensors and the ability to control the car accordingly is essential [1]. Significant effort has been dedicated to the design of vision-based autonomous driving systems thanks to the recent advancement in computer vision. In general, such research can be divided into two categories. The first way is to deploy geometric analysis algorithms to create a model of the vehicle's surrounding environment, which is then used for planning and control [2]. The second way is to learn a policy that directly maps the sensory input, such as the live feed from a front-facing camera, to a set of control commands by imitating an expert driver [3]. We follow the latter as it allows the system to directly extract features from the input that is relevant to the control problem, thereby facilitating suitable features to be extracted.

In order to mimic expert drivers, imitation learning has been applied to a variety of driving tasks, including articulated motion [4], road following [3, 5] and obstacle avoidance [6, 7]. The control policy is typically trained using supervised learning, where expert reference is provided. The system performance is improved by automatically learning the necessary internal representation from raw sensory input. Compared with rule-based solutions [2, 8], imitation-learning systems are capable of recognising visual cues that might be difficult to anticipate, allowing it to understand features that could have been missed by human drivers.

The recent development of deep learning has significantly improved the control quality in imitation learning. Bojarski *et al.* [3] utilised synthetic images to train an end-to-end system, which deduces the shift and rotation required for a scenario according to the recorded control signals. Toromanoff *et al.* [5] used a lateral control model to generate failure cases of driving, such that machine-learning systems can learn how to recover from failure cases. More recent works leverage auxiliary tasks for feature learning. Tasks such as segmentation [9] and optical flow estimation [10] can be applied to enhance the quality of training for

the vehicle control prediction problem. Furthermore, multi-task frameworks have been shown to be effective in controlling multiple aspects of driving at the same time. Chowdhuri *et al.* [6] trained the system to predict the steering angle and speed simultaneously using the multi-task learning framework. They collect recovery data in real sites as special driving behaviour. Yang *et al.* [11] also trained a multi-task network to regress control commands and use the inferred speed to compute the recovering label. In particular, temporal information has been taken into consideration for further improving the robustness in autonomous driving. Some researchers proposed using long short-term memory (LSTM) in their deep-learning frameworks to infer steering angles [9, 10, 12]. However, while these methods work well under normal circumstances, relying on a period of temporal information for driving controls could be risky as unexpected discrete events such as a car crash can happen instantaneously. How to apply temporal information to the best use remains an open problem.

In this paper, we propose a new framework for controlling self-driving cars utilising *optical flow* [13] as a core feature to represent motion cue, as shown in Fig. 1. Such features are powerful for control tasks, as they encode the per-pixel movement between two consecutive images. This allows an effective mapping between the features and the control signals. Building around the optical flow feature, we propose a deep-learning system to generate the control signals. As the flow can encode the temporal information between two frames, our system does not need a recurrent module [9, 10, 12], although we can include such modules for considering a longer temporal duration. The frame-based nature of our system allows the system to react quickly to unexpected events.

Our framework has two major components. The first component is the flow predictor. As opposed to the approach in [6, 9], our model does not require expensive annotations for the flow prediction task. This is made possible by a self-supervised mechanism [14] to model the underlying scene structure observed from consecutive frames and to generate the optical flow. The second component is the controller, which is a supervised convolution neural network. Its task is to learn the mapping between the input flow and the control signals. Motivated by the



**Fig. 1** Optical flow feature as a better cue for learning control signals. We proposed to generate the optical flow feature (upper) that highlights movement across frames from a colour dash camera frame (lower). Such a feature is a powerful cue in learning self-driving car controls

previous success of previous work [6, 11], we design the controllers as a multi-task deep-learning structure to simultaneously estimate the control speed and yaw rate. Our multi-task setup generates slightly superior results than the single-task one. It is also able to generate both control signals within the same architecture, which ensures that the two signals agree with each other to form a coordinated control strategy.

To evaluate the proposed self-driving model, the Cityscapes data set [15] is used. The results demonstrate the effectiveness of the use of optical flow in self-driving car controls. We outperform Bojarski *et al.*'s [3] steer prediction network by 48.9% in mean absolute error (MAE). Our multi-task network also demonstrates improvements over traditional single-task setups, boosting the MAE of steer prediction by 5.8%.

The main contributions of the proposed paper are:

- (i) We propose a new framework that utilises optical flow as a motion cue for self-driving car controls. We demonstrate that the feature is effective in improving the accuracy of the control signal, and our deep-learning system outperforms existing methods significantly.
- (ii) We propose a multi-task deep neural network to predict both the yaw rate and speed from the optical flow input. We show that the multi-task setup not only performs slightly better than the traditional single-task one but also capable of generating both controls under the same architecture, ensuring the coherence of the control strategy.

The rest of the paper is arranged as follows. We first review previous work in Section 2. We explain our flow-feature informed framework including a flow predictor and a controller in Section 3. We present the Cityscapes data set used in our experiment in Section 4 and show the results of our proposed systems in Section 5. Finally, we conclude the paper and discuss possible future directions in Section 6.

## 2 Related work

In this section, we review some prior research that is closely related to our work. We first cover learning based methods used for vehicle steering control, as well as the data required for training the system. We then discuss the extraction methods of optical flow features particularly on self-driving applications.

### 2.1 Deep learning for self-driving

Recently, as a promising approach, there is a growing interest in imitation learning to train self-driving systems. Bojarski *et al.* [3] proposed a deep-learning framework with convolutional neural networks (CNNs) that parsed high-dimensional camera inputs through some convolutional layers into the driver's actions. The proposed system learns the internal representations of useful visual

cues, such as road signs and objects, from the input images. It then correlates them with a simple control signal (i.e. the steering angle) during the training stage. This allows training for the driving policy effectively. Codevilla *et al.* [7] proposed a CNN framework that exploited the expert's intention representations in addition to front images for predicting the vehicle speed and steering angle. The proposed conditional imitation-learning framework takes a high-level command together with the corresponding front image as the input to guide the vehicle, allowing controls such as deciding the turning direction in an upcoming intersection. Similarly, Chowdhuri *et al.* [6] used mode indicators as the second input in their CNN training. Specifically, three behavioural modes, namely *direct*, *follow* and *furtive*, were used in training the networks as a multi-modal multi-task learning problem. Such a secondary high-level input command enables the change of driving behaviour. It also provides the system with more flexibility and can potentially adapt better to different situations. We also use CNN in our work to extract information from the optical flow feature and the camera image.

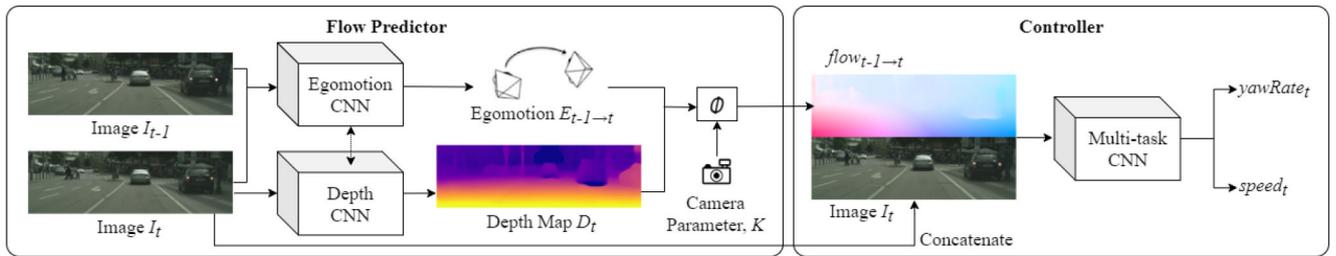
Xu *et al.* [9] developed a framework that integrates CNN with LSTM. It learns jointly from control loss and image segmentation loss to predict control commands based on a sequence of camera frames. The main difference between their work and the prior ones is the use of uncalibrated, crowd-sourced video data in the training stage. Although this makes the model training more challenging, the trained models are more robust in different situations. They further contribute to the community by making their large-scale annotated video data set, the Berkeley DeepDrive Video Data set, available to the public. We use optical flow to represent the per-pixel movement between two frames, and we achieve good results without the use of LSTM, although our design is compatible with it.

To provide the passengers and practitioners with more insight into the learned driving policies, Kim and Canny [12] implemented a CNN with attention model and exploited visual explanations to interpret the steering angle predictions. In particular, the regions on the image that are influencing the driving control signals are highlighted. Recently, the authors in [16] presented a new framework to generate textual explanations for their self-driving systems. On top of applying the attention-based models to understand the relationships between visual cues and driving control commands, the system also provides a textual description for a corresponding video. Bojarski *et al.* [17] also proposed a method to visualise the intermediate layers to explain their CNN framework PilotNet in [3]. The key idea is to find the salient objects that are the most influential to the driving commands in the road image. Due to the simplicity of the method compared with existing saliency detection approaches such as sensitivity-based and deconvolution-based approaches, the system is fast enough to be used on the NVIDIA DRIVETM PX 2 AI car computer.

### 2.2 Data for training

Training data has been a common problem for different learning techniques. Several large-scale data sets are developed to enable supervised learning in autonomous driving. Some aforementioned approaches, such as [9, 12], were tested on public data sets that include dash camera videos with time-synchronised speed and steering commands recorded from human drivers, including the BDD100k [18] and the comma.ai data sets [19]. The KITTI data set [20], which is the main benchmark for autonomous driving, has the front image sequences along with the camera pose. The Cityscapes data set [15] is another benchmark. It contains preceding video frames and the time-synchronised speed (m/s) and yaw rate (rad/s). Combining them allows the calculation of the vehicle trajectory based on the kinematic model in [21]. In this research, we train our model to recognise the change in the vehicle's movement from flow features such as rapid acceleration or sharp turns. Therefore, the Cityscapes data set [15] was used as it comes with the time reference.

Unbalanced training data has introduced risks of generating unexpected control behaviours [22]. The data are captured from human drivers, and in most of the cases, they are driving on a



**Fig. 2** Overview of our optical flow informed self-driving framework. Our framework consists of a flow predictor and a driving controller. The flow predictor estimates the depth image and the egomotion (i.e. camera motion) from consecutive monocular dash camera frames to calculate the optical flow. The flow and the current camera image are strong features representing the current scene. They are concatenated as the input of the driving controller, which deduces the control signals yaw rate and speed

desired trajectory. These data result in a dominating amount of *normal behaviours* data, and the systems have little chance to learn about recovering the vehicle from abnormal situations. Furthermore, in autonomous driving, latent shifts accumulate over time leading to the vehicle driving away from the expert trajectory [6]. The accumulated prediction error in vehicle steering angle eventually causes the vehicle to drift off the road. To tackle the problem of data bias and error accumulation, synthetic images corresponding to lateral failure cases were created to train the neural networks in [3, 5]. Reinforcement learning can be used to reduce the amount of training data needed, which rely on trial-and-error instead of pre-recorded data for training. The approaches have been used to approximate the observed values, for state or goal [23]. Still, the nature of reinforcement learning is infeasible for real-world driving due to the potential danger to road users. As a solution, Pan *et al.* [24] trained a driving policy by reinforcement learning in a virtual environment and adapted it to the real world. Since there was a large difference between the real-world road image and the virtual-world synthesised image, a generative adversarial network (GAN)-based image translation network was proposed for image conversion. In this work, we do not focus on the data imbalance problem, but our framework is compatible with GAN for tackling it.

In autonomous driving, the visual feedback is obtained in a sparse manner and is abstracted representing knowledge as a key to an effective reinforcement-learning process. To tackle this problem, Kulkarni *et al.* [25] combined hierarchical approaches with deep reinforcement learning to control agents. Agent behaviours and goals were simultaneously learned from experience with two levels of hierarchy. For compound learning, multiple inputs were often fused into a shared representation through concatenation [26]. This shared representation was then learned to infer the expected goals. We also apply data concatenation to combine the use of the captured colour image and its corresponding optical flow for generating the control signals.

### 2.3 Optical flow

The essential cues for self-driving in dynamic scenes, such as physical scene constraints, spatial patterns and existence of objects, can be obtained based on relative motion between the camera and the scene. Optical flow serves as an effective representation to estimate such information [13]. It represents the pattern of object movement over time, mostly considering two consecutive image frames [27]. It is more challenging to adapt it to outdoor environments, where the scene contains more local ambiguities resulted from reflective surfaces and less-textured surfaces [28]. This is because local features are fundamental factors for matching pixel patches when estimating the flow. One possible solution is to make use of the depth information on continuous objects which provides strong geometric cues for matching pixels in neighbouring frames [29].

Optical flow has been used heavily in a wide variety of applications particularly in self-driving [30]. Kashyap *et al.* [31] estimated optical flow from a front-view camera. They separated the flow into the image velocity component and the object motion using the camera motion estimated from a deep network. Hou *et al.* [10] proposed to utilise two pre-trained auxiliary networks, one for

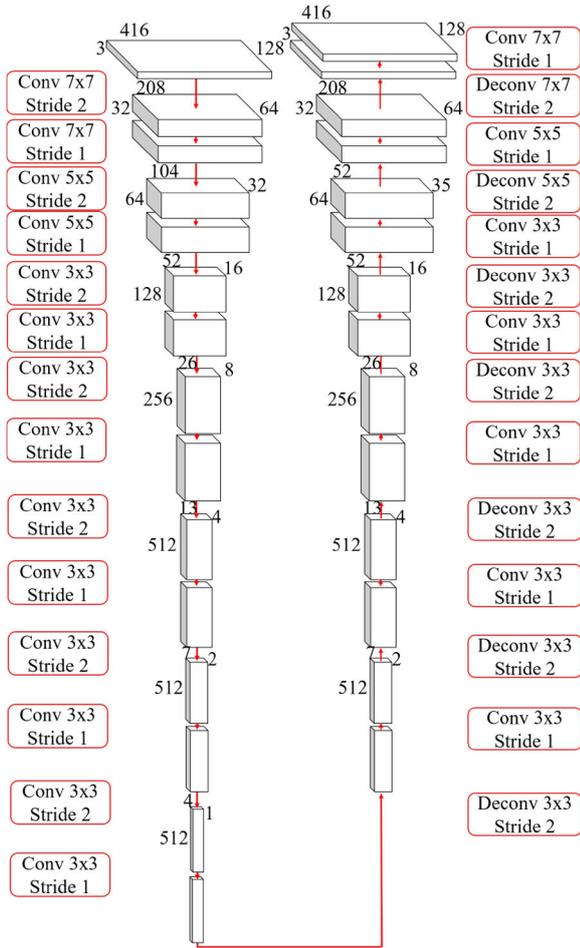
image segmentation and one for optical flow prediction, to guide the main encoder network to generate low-dimensional deep feature, which is then inputted to an LSTM module for predicting the control signals. We believe that the use of the LSTM module to model temporal information may not be necessary, as the optical flow features already define the movement feature across time effectively. We, therefore demonstrate that by using optical flow directly as the input, control signals can be accurately predicted. We further propose a multi-task structure that utilises two sub-branches to predict two different control signals, the steering angle and speed, as opposed to [10] that outputs them in the same layer. Due to the use of individual subbranches, our system has a better capacity to generalise to control signals in which angle and speed are in some unusual combinations.

To further improve the performance of autonomous driving, researchers have been trying to estimate the three-dimensional (3D) location of the vehicle from the ego-centric video captured from the dash camera. This can be done by estimating the camera pose (including both the location and orientation) and the spatial information between the vehicle and the environment. Such information is taken into account when learning driving policies. Zhou *et al.* [14] used an explainability mask to exclude moving objects from dashcam videos. They created an unsupervised framework to simultaneously estimate the depth map and the camera egomotion with two CNNs. Remarkably, they achieved better camera pose estimation results compared with the established SLAM system. We utilised the literature work [14] to estimate the depth map and egomotion, which are then inputted to an analytical algorithm to calculate the optical flow. By modelling the scene and the dynamic objects, Casser *et al.* [32] improved Zhou's work by incorporating a 3D object motion estimators and achieved better results, egomotion prediction very close to the ground truth odometry and proposed a refinement method applicable to fine-tune the result in an online fashion. To jointly estimate depth and camera motion, it is common to assume that the scenes are mostly rigid. Ranjan *et al.* [33] used a competitive collaboration framework to reason about every pixel across the image (i.e. static or not), by exploiting low-level information like depth, camera motion and optical flow. In this research, we train a CNN controller to distinguish which of the pixel displacement is dominated by the camera motion.

## 3 Optical flow informed framework

We propose a deep neural network framework that consists of a flow predictor and a driving controller. The former is to construct the optical flow features, while the latter use such features to deduce driving control signals.

The overview of our framework is shown in Fig. 2. Given two consecutive frames  $I_{t-1}$  and  $I_t$  from the dash camera, the flow predictor estimates the depth images  $D_t$  at frame  $t$  and the egomotion (i.e. camera motion)  $E_{t-1 \rightarrow t}$  from frame  $t-1$  to frame  $t$ , based on two jointly trained self-supervised CNNs. The depth image and the egomotion are used to calculate the optical flow image  $flow_{t-1 \rightarrow t}$  from frame  $t-1$  to frame  $t$ . The flow image is spatially concatenated with the current frame  $I_t$  to form the input of the controller, which is a supervised multi-task CNN to predict the



**Fig. 3** Depth CNN for estimating the depth map The depth CNN has an encoder–decoder architecture, with the input layer (top left block) being the colour image and the output layer (top right block) being the estimated depth image

driving control commands, including the yaw rate  $\text{yawRate}_t$  and the speed  $\text{speed}_t$ .

There are two major design concepts in our framework. The first one is that the front-view images and the motion-based cues between consecutive frames (i.e. optical flows) serve as a powerful representation of the current scene. Comparing with methods that do not explicitly represent the motion cues [3, 5, 12], our system performs more robustly, with the control signals predicted more accurately. The second key design is to directly use the image-based input generated from the monocular dash camera to train the control policy. Unlike existing work that applies prior knowledge to model the scene [9, 11], our framework ensures that the control policy is informed by all features obtainable from the image and flow with the least amount of user intervention.

### 3.1 Flow predictor

The flow predictor generates the optical flow image from two consecutive frames  $I_t$  and  $I_{t-1}$ , as shown in the left part of Fig. 2. To do so, we first utilise the method proposed in [14] to estimate the camera egomotion and depth map from the two frames. We then introduce an analytical algorithm to calculate the optical flow from the estimated egomotion and depth map.

Here, the dash camera should be set up to obtain a clear view with little occlusion, so that the camera motion can be effectively estimated from image features such as the geometry of the streets. An unoccluded scene is also a pre-condition for human driving, and the vast majority of available data sets fulfil this condition.

#### 3.1.1 Self-supervised CNNs for egomotion and depth: The flow predictor consists of two deep CNNs for two different tasks.

First, the depth CNN is a convolutional encoder–decoder architecture producing a dense depth map from a single RGB image. That is, it takes the frame  $I_t$  and estimates the depth map  $D_t$ . As visualised in Fig. 3, the input layer from the top left block is the RGB image. A series of convolution layers shown in the left branch reduces the images to a low-dimensional deep feature (lower left block). Then, a series of deconvolution layers shown in the right branch restores the deep feature into the original dimensionality (upper right block), with the nature of the images being converted into the depth map. In this network, the convolution layers are in pairs, consisting of one layer with a stride of 2 and another with a stride of 1. The former reduces the dimensionality of the feature, while the latter improves the generalisation power of the network.

Second, the egomotion CNN takes a sequence of two RGB frames as the input and produces a six-degree-of-freedom (DoF) transformation vector between the frames as the output, represented as 3D translation and 3D rotation. That is, it takes the frames  $I_t$  and  $I_{t-1}$  to estimate the egomotion, which is the camera motion,  $E_{t-1 \rightarrow t}$ . As visualised Fig. 4, the input layer is the image formed by concatenating  $I_t$  and  $I_{t-1}$  (top left block). The left branch is an encoder–decoder structure that reduces the image into a low dimensional deep feature (middle left block). Such a feature is passed into the right branch with future convolution layers to regress the six DoF camera egomotion vector.

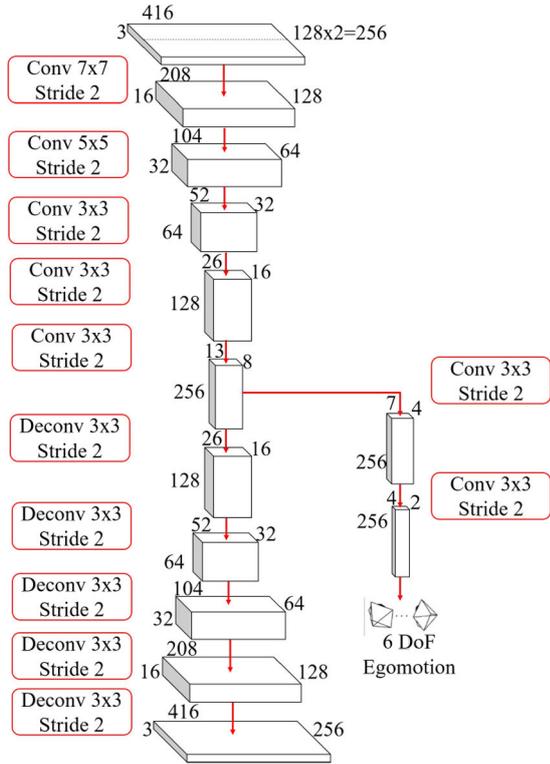
The two networks are trained together such that the overall system is self-supervised. We implement a differentiable image warping operator  $\psi$  that reconstructs a target image from a source image with a camera motion. In each epoch, using  $\psi$ , the inverse of the egomotion  $E_{t-1 \rightarrow t}$  is applied on the RGB image  $I_t$  with geometry information from the depth image  $D_t$  to recreate the projected version of the frame  $I_{t-1}$ , which we called  $I_{t-1-t}$ . Such a projected frame is compared with the original image  $I_{t-1}$  using a photometric loss in the RGB space to construct the self-supervise signal:

$$\text{Loss} = \| I_{t-1-t} - I_{t-1} \| \quad (1)$$

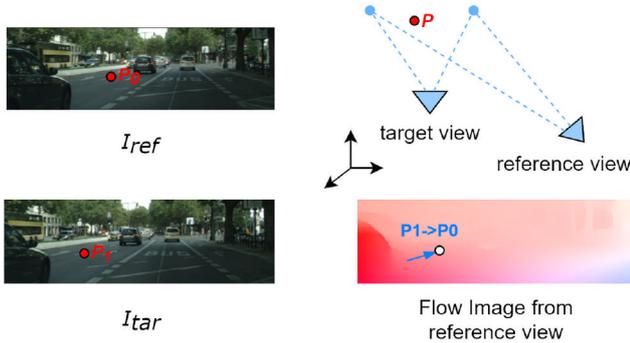
The loss informs the performance of both the egomotion CNN and the depth CNN, and is used to train both systems. Regarding the implementation, we scale the images in our data set to fit the input dimensions of the depth and pose networks, which helps to avoid changing the network structure.

**3.1.2 Optical flow calculation:** A major requirement for self-driving systems is to understand highly dynamic environments and extract robust features. This motivates us to represent the motion features using dense optical flow, which indicates the displacement of all pixels between two consecutive frames. On the one hand, traditional colour images, depth images segmentation features used in self-driving vehicles [14, 34] can only represent a static frame. Therefore, they typically require the deep-learning network to include a temporal module such as LSTM [10] for understanding motion and predict the control signals. With the optical flow that represents motion features directly, we demonstrate that the temporal module is not necessary for our system. On the other hand, traditional features for temporal tracking such as HOG and HOF are 2D in nature, and the tracking performance depends heavily on whether distinctive feature points are available [35]. Our optical flow is calculated by first projecting the 3D point cloud from the depth image with the camera egomotion, and then mapping the angle and magnitude of the per-pixel 3D motion into the 2D colour space, as shown in Fig. 1 as an example. Therefore, our optical flow represents dense 3D motion features for self-driving controls.

As illustrated in Fig. 5, when an observed point  $P$  on a surface remains static between the two frames, the observed optical flow is purely driven by the camera motion. For the sake of better understanding, an example of a car turning right and merging into a traffic lane is used here. Point  $P$  is a static point on the road surface. The pixel point  $P_0$  is the point  $P$  from a reference view  $I_{\text{ref}}$ . The pixel point  $P_1$  is the point  $P$  from a targeted view  $I_{\text{tar}}$ . Since the



**Fig. 4** Egomotion CNN for estimating the camera egomotion. The egomotion CNN has an encoder–decoder architecture as shown in the left branch, with the input layer (top left block) being the two concatenated colour images and the output layer (lower right block) being the estimated six DoF camera egomotion



**Fig. 5** Geometric relationship between reference and target views. Given a car is turning right and merging into a traffic lane. Point  $P$  is a static point on the road surface. The pixel point  $P_0$  is point  $P$  from a reference view  $I_{ref}$ . The pixel point  $P_1$  is point  $P$  from a targeted view  $I_{tar}$ . The flow image is from the reference view  $I_{ref}$

camera moves along with the car, the pixel point  $P_0$  moves to  $P_1$  accordingly.

More specifically, we calculate the optical flow field due to the camera motion. Given two consecutive images  $I_{t-1}$  and  $I_t$ , we first estimate the depth map  $D_t$  and the relative camera pose  $E_{t-1 \rightarrow t}$  by the self-supervised CNNs and (2) mentioned in Section 3.1.1. We then calculate the optical flow:

$$\text{flow}_{t-1 \rightarrow t} = \phi(D_t, E_{t-1 \rightarrow t}, \mathbf{K}) \quad (2)$$

where  $\phi$  is an analytical algorithm,  $\mathbf{K}$  is a matrix representing the camera's intrinsic parameters.

The algorithm  $\phi$  can be broken down into multiple key steps. First, we create two matrices  $\mathbf{u}$  and  $\mathbf{v}$  that represent pixel displacement along the  $x$  and  $y$  axes, respectively:

$$\mathbf{u} = \begin{bmatrix} 0 & 1 & \dots & w \\ 0 & 1 & \dots & w \\ & & \ddots & \\ 0 & 1 & \dots & w \end{bmatrix}, \mathbf{v} = \begin{bmatrix} 0 & 0 & \dots & 0 \\ 1 & 1 & \dots & 1 \\ & & \ddots & \\ h & h & \dots & h \end{bmatrix} \quad (3)$$

where  $w$  and  $h$  are the width and height of the input image  $I_{t-1}$  and  $I_t$ . We then use  $\mathbf{u}$  and  $\mathbf{v}$  to represent the depth map  $D_t$  in a point cloud representation consisting of the  $x$ ,  $y$  and  $z$  components:

$$\mathbf{PC} = [\mathbf{PC}_x, \mathbf{PC}_y, \mathbf{PC}_z, 1] \quad (4)$$

where

$$\mathbf{PC}_x = D_t \odot \mathbf{u}$$

$$\mathbf{PC}_y = D_t \odot \mathbf{v}$$

$$\mathbf{PC}_z = D_t$$

where  $\odot$  represents the element-wise multiplication. On the other hand, we estimate the normalised camera egomotion considering the intrinsic parameters  $\mathbf{K}$ :

$$\hat{E}_{t-1 \rightarrow t} = \mathbf{K} \cdot E_{t-1 \rightarrow t} \cdot \mathbf{K}^{-1} \quad (5)$$

where  $\mathbf{K}^{-1}$  denotes the inverse of  $\mathbf{K}$ . We then project the point cloud with the normalised egomotion to obtain the movement matrix:

$$\hat{\mathbf{PC}} = \hat{E}_{t-1 \rightarrow t} \cdot \mathbf{PC}^T \quad (6)$$

where  $\mathbf{PC}^T$  denotes the transpose of the  $\mathbf{PC}$  matrix. Finally, the two components of the optical flow are calculated as:

$$\text{flow}_{t-1 \rightarrow t, u} = \frac{\hat{\mathbf{PC}}_x}{\hat{\mathbf{PC}}_z} - \mathbf{u} \quad (7)$$

$$\text{flow}_{t-1 \rightarrow t, v} = \frac{\hat{\mathbf{PC}}_y}{\hat{\mathbf{PC}}_z} - \mathbf{v} \quad (8)$$

where  $\mathbf{PC}_x$ ,  $\mathbf{PC}_y$  and  $\mathbf{PC}_z$  are the  $x$ ,  $y$  and  $z$  components of  $\mathbf{PC}$ , respectively. The 2D flow image  $\text{flow}_{t-1 \rightarrow t}$  is represented by mapping the angle and the magnitude of the optical flow into the colour space.

The flow  $\text{flow}_{t-1 \rightarrow t}$  and the image  $I_t$  are considered as strong features and are used as the input of the CNN-based controller network.

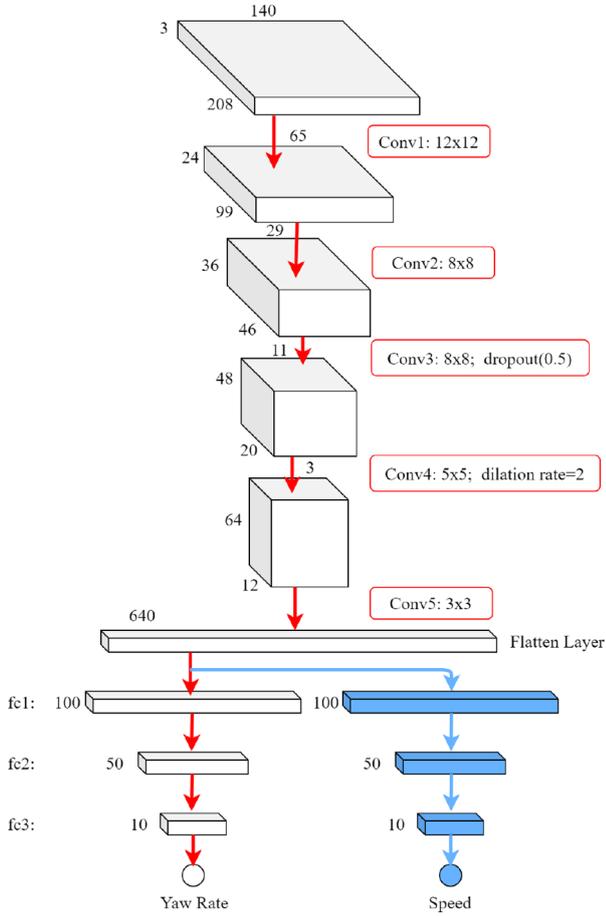
In addition, following [14], we implement a depth smoothing strategy. Specifically, we trained our flow predictor on the KITTI data set [20] and then applied the online refinement technique proposed in [32] to fine-tune the flow prediction module in this work. We found that the predicted flow fields successfully reflect the scene level consistent movement governed by the camera motion.

### 3.2 Controller network

In this section, we explain the controller network that predicts the control signals yaw rate and speed through multi-task network architecture. Such an approach improves the generalisation and exploiting commonalities between the two tasks in order to achieve a better performance in controlling the vehicle.

We adopt the end-to-end CNN architecture in [3], as its effectiveness in mapping raw pixels directly to vehicle control signals has been demonstrated. The end-to-end architecture means that images features are mined directly from the raw input with minimal human interventions.

We modify the architecture in [3] to create our controller network by introducing a multi-modal multi-task CNN structure, as



**Fig. 6** CNN architecture for our controller module. The network takes multi-modal input (i.e. image and optical flow) and performs multitask control prediction (i.e. yaw rate and speed)

shown in Fig. 6. From the top of the image, the network takes the concatenated image of the current image,  $I_t$ , and the optical flow,  $\text{flow}_{t-1 \rightarrow t}$  as the input, which is a three-channel RGB image. The five convolution layers extract the image features that are useful to our task. The flatten layer generate a 1D vector that represents the deep features. Then, the left-hand side part of the network coloured in white consisted of three fully connected layers, generates the yaw rate,  $\text{yawRate}_{t \rightarrow t+1}$ . The right-hand side part coloured in blue, consisted of three fully connected layers as well, generates the speed,  $\text{speed}_{t \rightarrow t+1}$ .

This multi-task structure allows the system to model the correlation between different tasks, which are the steering angle and speed in our case. The shared layers are used to model common knowledge between the two tasks, while the separate sub-branches are used to model the task-specific knowledge. During backpropagation, the ground-truth signal of each task updates both the shared layers and its task-specific branch. Through the shared layers, the knowledge between the two tasks is generalised.

The loss function of our framework is defined as the mean absolute error between the predicted yaw rate  $\text{yawRate}_{t \rightarrow t+1}$  and the ground truth  $\text{yawRate}'_{t \rightarrow t+1}$ , together with that between the predicted speed  $\text{speed}_{t \rightarrow t+1}$  and the corresponding ground truth  $\text{speed}'_{t \rightarrow t+1}$ :

$$\text{Loss} = \alpha_1 \|\text{yawRate}_{t \rightarrow t+1} - \text{yawRate}'_{t \rightarrow t+1}\| + \alpha_2 \|\text{speed}_{t \rightarrow t+1} - \text{speed}'_{t \rightarrow t+1}\| \quad (9)$$

where  $\alpha_1$  and  $\alpha_2$  are the parameters to balance the influence of yaw rate and speed loss, respectively, on the prediction task. An ablation study with different loss weight ratios  $\alpha_1/\alpha_2$  has been conducted to find out the best prediction performance, which is described in Section 5.

Furthermore, in terms of implementation, different from the CNN architecture in [3], we adopt a larger kernel size of  $12 \times 12$  in the first few convolutional layers. This is driven by the observation that larger kernels are more suitable for environmental contexts extraction from front-view cameras [11]. Bojarski *et al.* [3] resizes the input to  $66 \times 200$  pixels, which limits the network's ability to learn from smaller objects in the large scene. Motivated by [36] where contextual representations are learned from a large receptive field using dilated convolution layers, we increase the dilation rate in the convolutional operation, which allows learning from the images with less computational cost with larger dimensions of  $140 \times 208$  pixels.

**3.2.1 Baseline setup:** We set up a baseline network with only the yaw rate network but taking the multi-modal input of an image frame and the corresponding optical flow. This allows us to demonstrate the effectiveness of our multi-task architecture that considers both yaw rate and speed.

The baseline network is represented as the white part of the network in Fig. 6 without the blue part. The network still takes the multi-modal input of both the current image,  $I_t$ , and the optical flow,  $\text{flow}_{t-1 \rightarrow t}$ , but it only predicts the yaw rate,  $\text{yawRate}_{t \rightarrow t+1}$ .

The loss function is defined as:

$$\text{Loss} = \|\text{yawRate}_{t \rightarrow t+1} - \text{yawRate}'_{t \rightarrow t+1}\| \quad (10)$$

where  $\text{yawRate}'_{t \rightarrow t+1}$  is the corresponding ground-truth value.

## 4 Cityscapes data set

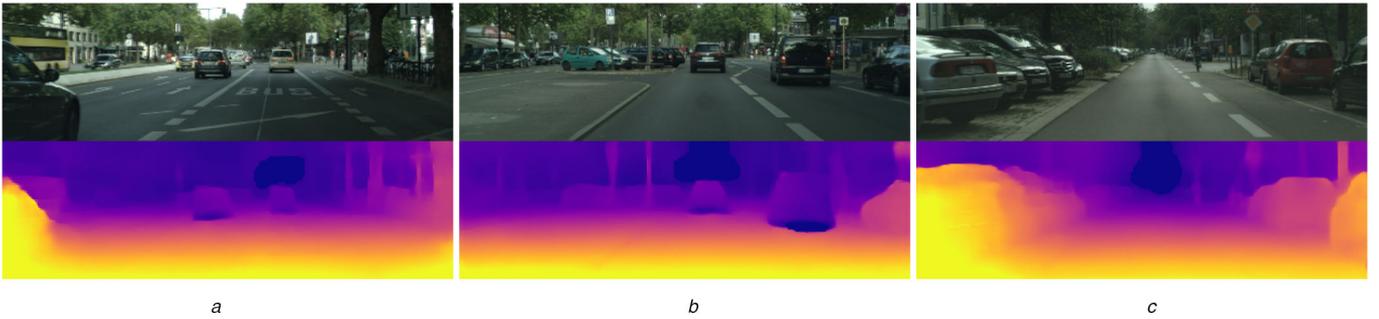
In this section, we introduce the benchmark Cityscapes data set [15] and the data pre-processing methods used in this work. Such a data set fits the best in our system for several reasons. First, Cityscapes provides both the vehicular ego motion data and the camera intrinsic parameters, which are both necessary information in our system. Other popular data sets such as BDD100 K [18] do not provide camera information. Second, it provides control information including both speed and steering angle, which is not present in other data sets such as KITTI [20]. Third, the data set consists of many rapid acceleration/deceleration periods and sharp turns in a complicated city environment, which serves as challenging scenarios for the system to learn the driving signal. In comparison, the comma.ai [19] data set consists of mainly highway scenarios, and the Ford Campus Vision and Lidar Data Set [37] consists of mainly straight roads. Both are considered to be less challenging.

The Cityscapes data set is a large-scale data set with mainly urban street scenes. It contains 5000 preceding video sequences and time-synchronised ego-motion parameters from the vehicle odometry including the speed (m/s) and the yaw rate (rad/s) annotation for every frame. Every video sequence has 30 frames collected within 1.8 s. As images sampled at a high rate would be highly similar and thus provide less useful information [3], we extracted pairs of images and ego-motion labels from each video sequence at the same sampling rate as in [32] for feature extraction. Furthermore, unnecessary parts of the images such as the automobile hood and the sky were cropped out to improve the efficiency of the training process. The resultant images are scaled for normalisation to match the input size of the networks.

Video sequences in the Cityscapes data set were collected in the daytime under good or medium weather conditions in 50 cities, with four types of camera intrinsic settings. Some examples of the contained street scenes with varying background and scene layout are shown in Figs. 7 and 8.

### 4.1 Annotating data using the speed ratio

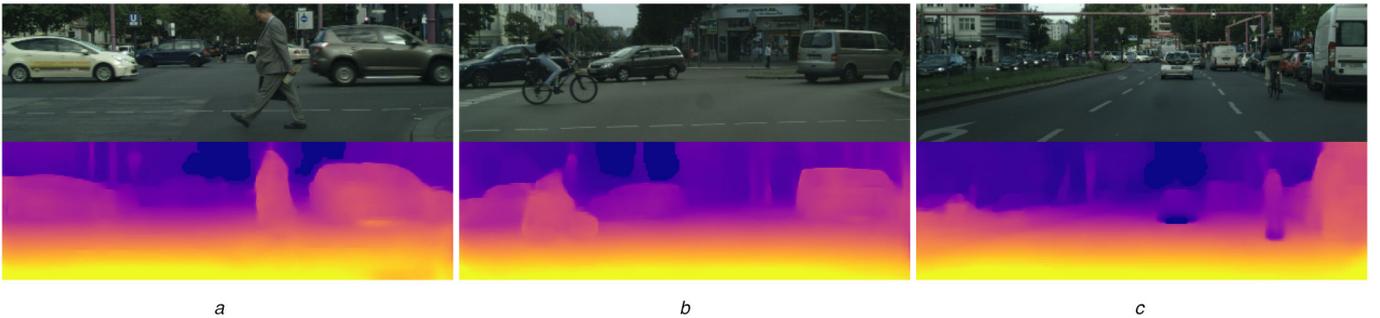
In order to make the control predictions smooth and confirm to motion laws, we tried to adopt the speed ratio that compares the speed of the current frame with the previous frame as the label as in [11, 16]. We would like our controller to regress a vehicle's movement trend  $\Delta s = s_t/s_{t-1}$  from the RGB image and the flow image, and then determine the speed  $s_t$  based on the vehicle's prior



**Fig. 7** Examples of depth maps computed from different situations  
 (a) Another car in proximity, (b) Typical traffic, (c) Lot of parked cars



**Fig. 8** Examples of flow features computed from different situations  
 (a) Pedestrians crossing the road slowly, (b) Low traffic, (c) Low traffic



**Fig. 9** Examples of depth maps computed from different situations  
 (a) With pedestrian, (b) More complicated scene with a cyclist, (c) More complicated scene with a cyclist

movement state  $s_{i-1}$ . For both of the aforementioned speed label preparation methods, the samples with a very low speed ( $<0.1$  m/s) are discarded to ensure a consistent driving condition. We demonstrate the performance gain and justify our choice in using speed ratio in an ablation study in Section 5.4.1.

## 5 Experimental results

In this section, both quantitative and qualitative experimental results are presented. In particular, we compare the proposed multi-task network with [3] and the baseline model explained in Section 3.2.1, demonstrating that our multi-task system performs the best.

### 5.1 Experiments setup

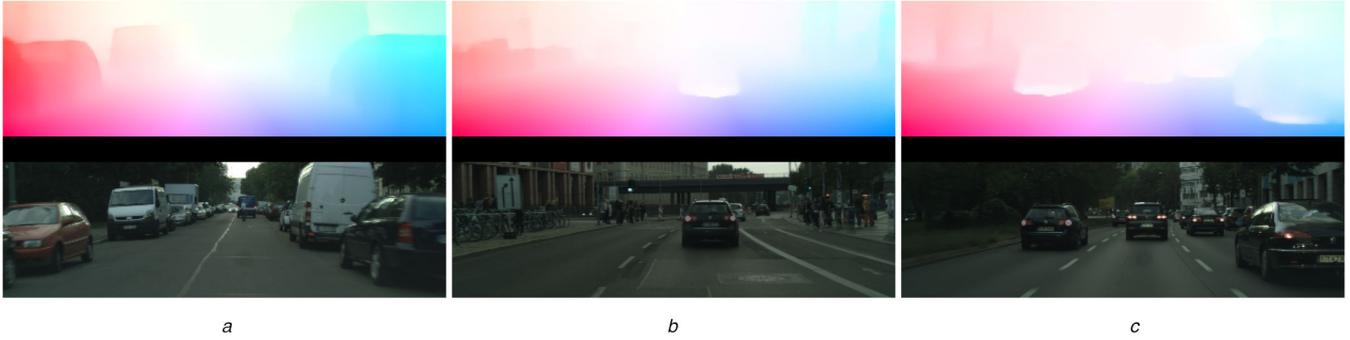
We used the same preprocessing settings and neural network hyperparameters for all the models. Samples were partitioned according to the setup of the Cityscapes data set (59.5% training, 10% validation and 30.5% testing) and were randomly shuffled. All the models were trained and tested using Keras utilising a Tensorflow backend on a GeForce GTX 1080 GPU-based system. We used the Adam optimiser with  $\beta_1 = 0.99$ ,  $\beta_2 = 0.999$  and a fixed learning rate of  $1 \times 10^{-4}$  in all experiments. The training time for the multi-task network was about 5 h for 30 epochs.

### 5.2 Qualitative evaluation

Some examples of video frames and the corresponding intermediate images (i.e. depth maps and flow features) are illustrated in Figs. 7–10 to demonstrate the high-quality results obtained using our proposed framework. In particular, brighter colour in the depth map denotes greater relative motion and shorter distance. Brighter colour in the optical flow features indicates a larger drift or movement. It can be seen that the extracted features are highly indicative of steering angle prediction (the going through and turning behaviours) in Figs. 9 and 10. In addition, the depth information on objects like cars, pedestrians and bicycles provides strong geometric cues for inference, which can be seen in Figs. 7 and 9.

The depth maps computed from a wide range of different situations are presented in Figs. 7 and 9. The samples in Figs. 7a–c clearly highlights that the spatial distances between the camera and other vehicles are estimated accurately. In Fig. 9a, it can be seen that the shapes and depth information of the objects (i.e. cars and pedestrian) is well-captured. We further show two challenging scenes in Figs. 9b and c in which a cyclist is included in the scenes with moderate traffic. Again, our proposed method extracted high-quality shape and depth information.

Examples of the flow features computed by our method can be found in Figs. 8 and 10. The results indicate that our method produces smooth and accurate flow features in different situations



**Fig. 10** Examples of flow features computed from different situations

(a) Lot of parked cars, (b) Cars moving together with higher speeds, (c) Cars moving together with higher speeds

**Table 1** Yaw rate and speed prediction errors with the proposed multi-task model on Cityscapes.

$\alpha_1:\alpha_2$	Yaw rate MAE, rad/s	Yaw rate RMSE, rad/s	Speed MAE, m/s	Speed RMSE, m/s
2:1	0.0132	0.0287	0.0632	0.0885
1:1	<b>0.0130</b>	<b>0.0281</b>	0.0649	0.0902
1:2	0.0132	0.0278	0.0635	0.0885
1:3	0.0135	0.0287	<b>0.0615</b>	<b>0.0867</b>
1:4	0.0139	0.0291	0.0627	0.0880
1:5	0.0146	0.0300	0.0627	0.0874
1:7	0.0148	0.0291	0.0629	0.0882

Bold values are best results.

**Table 2** Comparisons with [3] and baseline on Cityscapes

Model	Yaw rate	
	MAE, rad/s	RMSE, rad/s
Bojarski <i>et al.</i> 's model [3]	0.0270	0.0487
the baseline model (explained in Section 3.2.1)	0.0138	0.0282
the proposed multi-task model	<b>0.0130</b>	<b>0.0281</b>

Bold values are best results.

**Table 3** Comparisons with [34] on Cityscapes

Model	Yaw rate		Speed	
	MAE, rad/s	RMSE, rad/s	MAE, m/s	RMSE, m/s
single image [34]	0.0470	0.0759	2.6911	3.4776
stacked [34]	0.0246	0.0441	1.9261	2.5235
our model (1:1)	<b>0.0130</b>	<b>0.0281</b>	0.0649	0.0902
our model (1:3)	0.0135	0.0287	<b>0.0615</b>	<b>0.0867</b>

Bold values are best results.

consistently. When the cars are moving together at relatively high speed, the flow features indicates that correctly in Figs. 10b and c. The samples in Figs. 8a–c do not contain a lot of moving vehicles. As a result, the region surrounding the vanishing point will have larger changes and is indicated by a brighter colour in the flow features. Fig. 10a shows a traffic jam scenario with vehicles moving slowly. Similar to Figs. 8a–c the region surrounding the vanishing point will have larger movement.

### 5.3 Quantitative evaluation

**5.3.1 System performance:** The performance of the proposed multi-task model to predict both the yaw rate and speed on the Cityscapes data set is shown in Table 1. We show the mean average error (MAE) and root mean square error (RMSE) for the yaw rate and the speed ratio. It can be noted that the minimum yaw rate error is obtained with the weight ratio  $\alpha_1:\alpha_2 = 1:1$ , in which the MAE is 0.0130 and RMSE is 0.0281. The minimum speed error is

obtained with the weight ratio  $\alpha_1:\alpha_2 = 1:3$ , in which the MAE is 0.0615 and the RMSE is 0.0867.

It can also be observed that the weight ratio does not significantly increase the error, making it easy to pick the parameters that do well on both yaw rate and speed. For example, the parameter ratio 2:1, 1:1, 1:2 and 1:3 all generate good results in both yaw rate and speed, and they all outperform other methods we compare with. Such comparisons will be explained in the next section.

**5.3.2 Comparison with other methods:** We compare the proposed multi-task system with [3] and the baseline model as explained in Section 3.2.1 on the Cityscapes data set. Since both [3] and the baseline can only generate yaw rate, we optimised the models with respect to the yaw rate.

The result is shown in Table 2. Our optimised multi-task model outperforms both [3] and the baseline, with the smallest mean average error (MAE) and the smallest RMSE. The multi-task model is set up using the parameter ratio  $\alpha_1:\alpha_2 = 1:1$  and using the speed ratio as the target of the regression.

In particular, compared with [3], we observe an improvement in MAE of yaw rate from 0.0270 to 0.0130 rad/s, which is equivalent to a relative improvement of 48.9%. The RMSE is reduced from 0.0487 to 0.0282 rad/s, by 42.1%. It highlights the effectiveness of using flow features to help the model better understand the scene geometry and spatial pattern and thus generate a much more accurate yaw rate prediction.

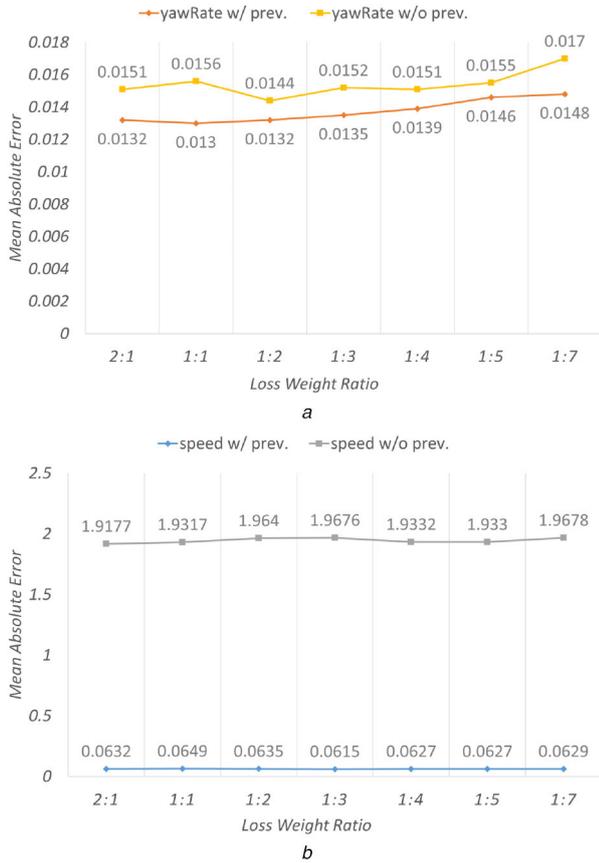
Also, compared with the baseline, the proposed system improved the MAE from 0.138 to 0.130 and RMSE from 0.282 to 0.281, despite the need to solving two tasks at the same time. This shows that the two tasks are highly relevant to each other. The proposed multi-task framework effectively solves them in the same network and generates better results.

While the best result for the yaw rate is obtained with the weight ratio  $\alpha_1:\alpha_2 = 1:1$ , we can see from Table 1 that even when we pick the weight ratio that is optimised for speed (i.e.  $\alpha_1:\alpha_2 = 1:3$ ), the proposed multi-task system still performs better than [3] and the baseline.

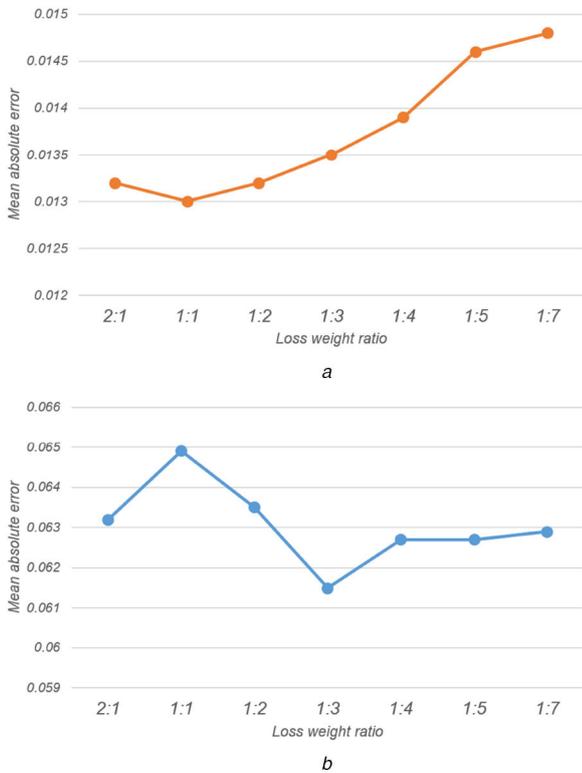
We further compare our work with [34], which achieved the second-best performance in the ICCV 2019 Learning to Drive challenge. It comes with the source code that we can use to retrain the network with the Cityscapes data set for experimental comparisons. We include both the single image (CNN\_SINGLE\_IMAGE) and stacked (CNN\_STACKED) implementations in [34] for comparison. As shown in Table 3, it can be seen that aligning with the findings in [34], the stacked implementation performs better. However, both networks cannot produce results as efficient as the results of our proposed system, either using the parameter ratio of 1:1 or 1:3. This indicates that the use of optical flow has a positive effect on estimating the control signals.

### 5.4 Ablation studies and parameter analysis

**5.4.1 Speed label preparation strategy:** Here, we further evaluate the performance of incorporating the multi-task model in the proposed framework. Specifically, this ablation test focuses on



**Fig. 11** Experiment results of multi-task network with/without using the speed ratio  
**(a)** Yaw rate prediction of multi-task CNN with different loss weight ratios, **(b)** Speed prediction of multi-task CNN with different loss weight ratios



**Fig. 12** Experiment results of multi-task network with different loss weight ratios for yaw rate and speed  
**(a)** Yaw rate prediction of multi-task CNN, **(b)** Speed prediction of multi-task CNN

the effect of the strategy of using the speed ratio annotated data in the proposed multi-task model.

For yaw rate prediction, as shown in Fig. 11a, the use of the previous dynamic state produced encouraging results by bringing down the yaw rate MAE for all the tests with different loss weight ratios. Without the use of previous dynamic state, the minimal MAE of 0.0144 was achieved when using 1:2 loss weight for yaw rate and speed prediction. With the use, the minimal MAE of 0.0130 was achieved when using 1:1 loss weight.

Similarly, for speed prediction, the use of previous dynamic state improved the results significantly in all weight ratios as shown in Fig. 11b. Without it, the minimal MAE of 1.9177 was achieved with the weight ratio of 2:1. With it, the minimal MAE of 0.0615 was achieved with the weight ratio of 1:3.

**5.4.2 Loss weight ratio:** Here, we present the results of an ablation study on changing the loss weight ratios in our multi-task model. The results are shown in Fig. 12. The best yaw rate prediction performance is achieved with the 1:1 loss weight ratio, while the best speed prediction is obtained with the ratio of 1:3.

Notice that our system performs generally well in the ratio range between 2:1 and 1:4. For example, using the ratio 1:1 where yaw weight achieves the best result, the speed error is only increased by 5%. Using the ratio of 1:3 where the speed achieves the best result, the yaw rate error is only increased by 4%. Finally, the ratio 1:2 results in a balance between yaw rate and speed.

## 6 Conclusion

Without learning from motion-based cues, vehicle control prediction networks are susceptible to complicated road scenes. In this paper, we develop a CNN framework to learn from dashcam videos and flow features between frames to predict driving control commands including yaw rate and speed. Our experiments show that flow features help the proposed approach to achieve a new state-of-the-art on the Cityscapes benchmark. With the speed prediction task, our multi-task network largely outperforms the previous steer prediction.

In the future, we are interested in implementing a driving test with a pre-recorded video in a simulator to further evaluate our work. Specifically, the simulator sends the first two frames of the test video to our trained model. The flow predictor creates the flow image and then the controller network infers the control commands for the second frame. The control predictions including speed and yaw rate are fed into the vehicle kinematic model [21] to compute the yaw and the displacement travelled by the virtual car. We will assume the ground is flat so we can transform the car's yaw and displacement in the world coordinate system to a camera motion in the camera coordinate system with camera calibration.

With the camera pose and multi-view images, we are able to synthesise a novel view for the updated position and orientation of the car. Ideally, the simulator then sends the new synthetic frame and the second frame to the model and the process repeats. Since the camera motion is available when creating the flow image and our model also predicts control commands based on the flow image, it is convenient to calibrate the lane centre associated with each frame and augment recovering data for failure case using the formula in [11]. By observing whether the simulated car would drift away in time, we will be able to evaluate the performance of the controller in managing to perform lane-keeping and car following tasks.

While this research can accurately predict the control signals from a video feed, control signal prediction is only one part of a fully self-driving vehicle system. When deployed onto a car, issues such as control signal delay and control noises would affect the system. With the use of driving simulation systems or even real cars, we may perform closed-loop tests to identify potential gaps in the control loop. In this aspect, we may also look into more dedicated control systems such as feedback controls to fill the gaps.

## 7 Acknowledgments

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